## Physics 3.4 : Demonstrate understanding of mechanical systems

## Level 3 Credits 6

This achievement standard involves knowledge and understanding of phenomena, concepts, principles and/or relationships related to translational; circular and rotational; and simple harmonic motion; and the use of appropriate methods to solve related problems.

Translational Motion
Centre of mass (1 and 2 dimensions); conservation of momentum and impulse (2 dimensions only).

Circular and Rotational Motion
Velocity and acceleration of, and resultant force on, objects moving in a circle under the influence of 2 or more forces, e.g. banked corners, vertical circles; Newton's Law of gravitation, satellite motion.

Rotational motion with constant angular speed and with constant angular acceleration; torque; rotational inertia; angular momentum; rotational kinetic energy; conservation of angular momentum; conservation of energy.

## Simple Harmonic Motion (SHM)

Displacement; velocity; acceleration; time and frequency of a particle undergoing SHM; forced SHM; resonance; the reference circle; phasors; conservation of energy.

Relationships:

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\begin{array}{lll}
d=r \theta & v=r \omega & a=r \alpha \\
\alpha=\frac{\Delta \omega}{\Delta t} & \omega=\frac{\Delta \theta}{\Delta t} & \\
\omega_{f}=\omega_{i}+\alpha t & \omega=2 \pi f & E_{\text {K(ROT) }}=\frac{1}{2} \mathrm{I} \omega^{2} \\
\tau=\mathrm{I} \alpha & \theta=\frac{\left(\omega_{i}+\omega_{f}\right)}{2} t & \omega_{f}{ }^{2}=\omega_{i}{ }^{2}+2 \alpha \theta \\
\theta & =\omega_{i} t+\frac{1}{2} \alpha t^{2} & \\
L=m v r & L=\mathrm{I} \omega \\
T=2 \pi \sqrt{\frac{l}{g}} & F_{g}=\frac{G M m}{r^{2}} & \\
y=A \sin \omega t & T & =2 \pi \sqrt{\frac{m}{k}} \\
& v & =A \omega \cos \omega t
\end{array} \quad a=-A \omega^{2} \sin \omega t
$$

$y=A \cos \omega t \quad v=-A \omega \sin \omega t \quad a=-A \omega^{2} \cos \omega t$

## MECHANICS: translation motion

By the end of this unit students should be able to:
$\square$ Describe translational motion using graphs, equations and words.
$\square$ Use free-body force diagrams to find resultant forces
$\square$ Calculate the centre of mass for a multibody system
$\square$ Analyse interactions by applying the idea of centre of mass.
$\square$ Describe the conservation of momentum with reference to the motion of the centre of mass of a system, when the motion of the particles is in one dimension
$\square$ Apply the principle of conservation of linear momentum in one and two dimensions including the use of vectors
$\square$ Understand the relationship between rate of change of momentum and force in one and two dimensions (Impulse)

## MECHANICS: rotational motion

By the end of this unit students should be able to:
$\square$ Understand Newton's laws of Gravitation, including the force on a satellite in a circular orbit

वAnalyse circular motion in terms of centripetal force, centripetal acceleration, period and frequency
$\square$ Define a gravitational field in terms of the force on a unit mass.
$\square$ Use Newton's law of Universal Gravitation to analyse the motion of satellites in circular orbit
$\square$ Analyse the Velocity and acceleration of , and resultant force on, objects orbiting under the influence of two or more forces (eg. Conical pendulums, banked corners)
$\square$ Describe and analyse rotational motion with constant angular acceleration and constant angular speed using angular quantities and rotational Kinematic equations
$\square$ Use rotational motion equations to solve problems (with constant angular acceleration)
$\square$ Describe torque as two equal and opposite forces producing rotational motion.
$\square$ Define Torque, rotational inertia, and the relationship between torque and angular acceleration
$\square$ Apply the principle of conservation of angular momentum to systems with no external torque.
$\square$ Apply the principle of conservation of energy to situations involving rotations to include rotational kinetic energy, conservation of gravitational potential energy, and rotational and translational kinetic energy.

## MECHANICS: Simple harmonic motion

By the end of this unit students should be able to:
$\square$ Investigate the features of Simple Harmonic Motion
$\square$ Describe Motion with a restoring force or torque proportional to displacement from an equilibrium position in systems such as mass-spring, pendulums, buoys
$\square$ Apply the equations describing SHM to calculate unknown physical quantities for displacement, velocity, acceleration and frequency of a particle undergoing simple harmonic motion.
$\square$ Use equations of motion for cases when the displacement at time zero is either maximum or zero (equilibrium position).
$\square$ Analyse real life situations of SHM including the use of the reference circle to analyse simple harmonic motion.
$\square$ Identify the kinetic and potential energies present at various positions/times of SHM (Conservation of energy)
$\square$ Understand the factors that determine resonant frequencies in physical systems.
$\square$ Describe situations involving Damped and forced oscillations; resonance

